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# A Coach's Experience Building a Thinking Classroom Lab in an Elementary School

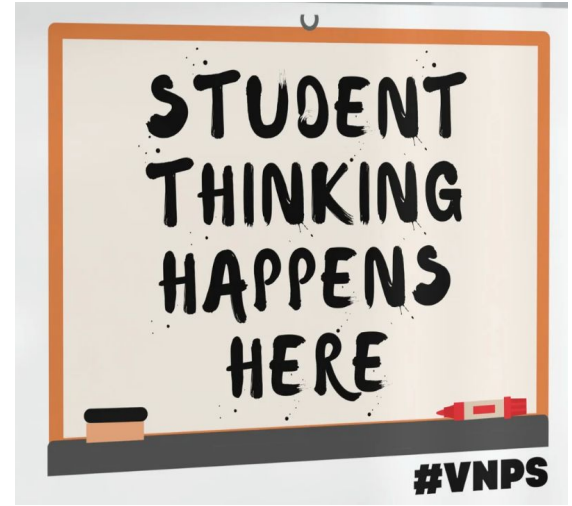
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# Agenda

- Overview of BTC philosophy
- Daniels Farm Teacher Learning
- Launch with non-curricular tasks
- Discourse
- Student Work
- Thoughts from students, teachers, and administrators
- Reflections



# Early Set-Up of Math Lab



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# 2022-2023 School Focus Statement

*“Thinking is a necessary precursor to learning, and if students are not thinking, they are not learning.”*

*- Peter Liljedahl*

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## Building Thinking Classroom

Defronted classroom



Students work at VNPS  
(vertical non-permanent surfaces)



Knowledge mobility



Assignments given orally



Visibly random groups



Work starts w/in 5 minutes



## Traditional Classroom

Teacher's desk is in front of the room

Students work at desks, seated

Teacher has all the knowledge

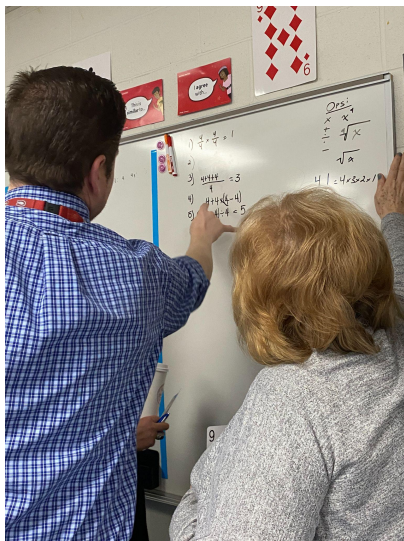
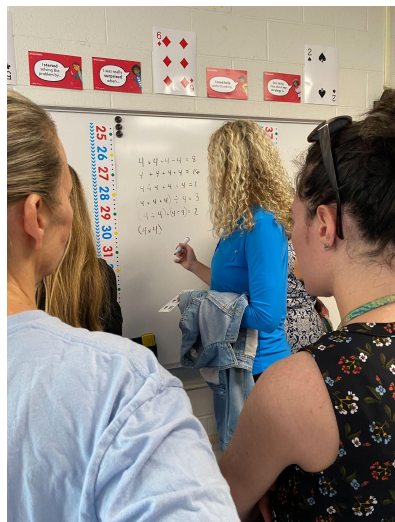
Assignments are taken out of the book

Students work independently

Students work after the "I do, we do"  
portion of the lesson

# 2022-2023 Math Lab Data

- Trimester 1 we had 92 lab visits
  - Trimester 2 we had 87 lab visits
  - All grades have been to the lab at least 6 times
  - The work in the lab includes tasks & thin sliced lessons
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# Teacher Learning

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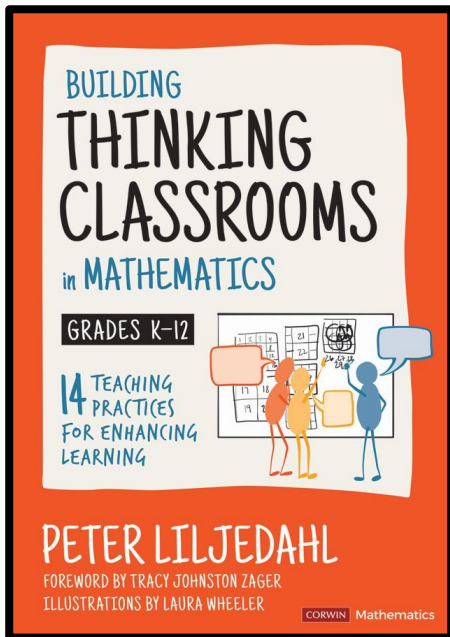
# Task

Find every number between 1 and 20 using only four 4s and any operation.

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# Thinking is the Goal



- Thinking vs. Studenting
    - **Trying it on their own** – attempting to work through a problem, regardless of whether they got it right or not
    - **Slacking** – not attempting to work at all
    - **Stalling** – doing legitimate off-task behavior
    - **Faking** – pretending to do the task but really doing nothing
    - **Mimicking** – mindlessly repeating what they have in their notes
-

# The Fourteen Practices - What Teachers Do

1. What types of tasks we use
2. How we form collaborative groups
3. Where students work
4. How we arrange the furniture
5. How we answer student questions
6. When, where, & how tasks are given
7. What homework looks like
8. How we foster student autonomy
9. How we use hints and extensions
10. How we consolidate a lesson
11. How students take notes
12. What we choose to evaluate
13. How we use formative assessment
14. How we grade



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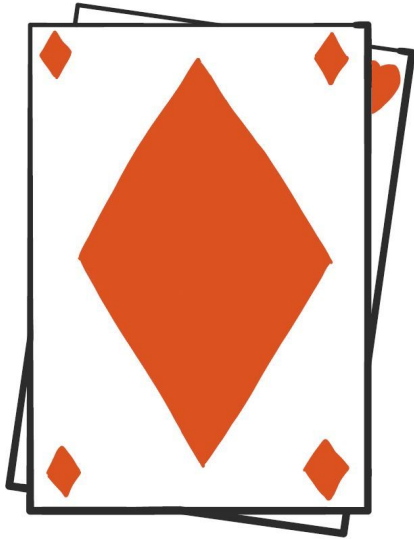
# 1. Types of Tasks We Use



- “Problem solving is what we do when we don’t know what to do.” - Peter Liljedahl
  - Begin with non-curricular tasks to establish norms
  - **Low-floor task** – anyone can get started with the problem
  - **High-ceiling task** – they have enough complexity to keep people engaged
  - **Open-middle** – while there is a single correct answer, there are multiple ways to solve the problem
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## 2. How We Form Collaborative Groups



- The groupings have to be visibly random
  - Grades 2+ - Three students is the ideal group size
  - Grades K & 1 - Two students is ideal group size
  - We like to say, “The cards have spoken.”
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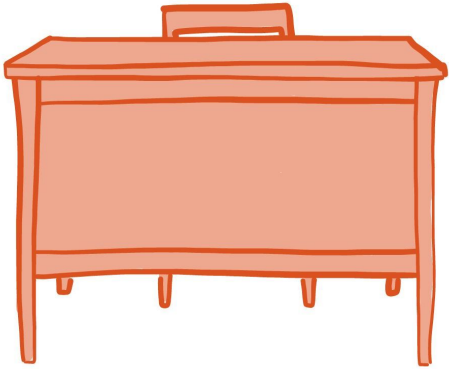
### 3. Where Students Work



- Sitting at desk writing in notebook is the LEAST conducive to thinking
  - Vertical Non-Permanent Surfaces (VNPS)
  - Non-permanent surface promoted more risk taking
  - Transformed passive environment into a thinking learning space
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## 4. How We Arrange the Furniture



- Defront the classroom
  - Teacher at front = teacher is knowledge
  - “Thinking is messy..... It turns out that in super organized classrooms, students don’t feel safe to get messy in these ways. The message they are receiving is that learning needs to be orderly, structured, and precise.” - Peter Liljedahl
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**Getting students started with  
non-curricular tasks**

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Presented to the kindergarteners orally:

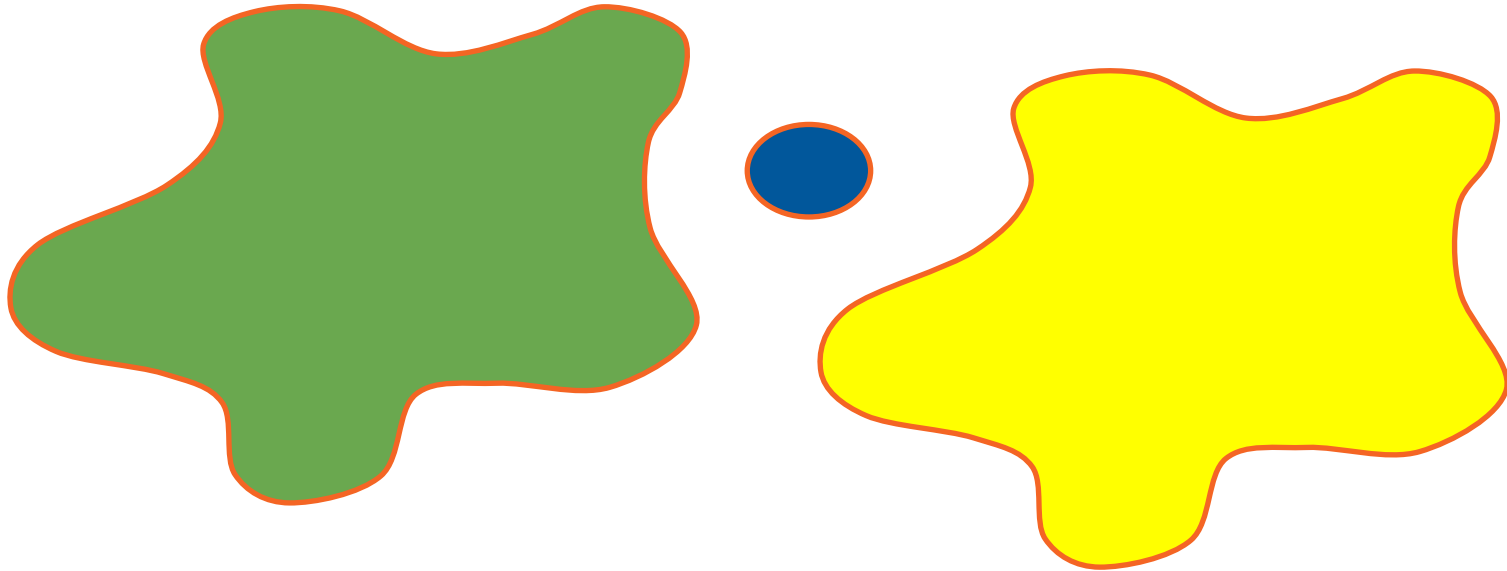
- What do you notice?
- What do you wonder?

Your job today is to draw 5 flowers with your partner.



9

Grade 1



Task: How many blue dots are under the green splat?  
How many blue dots are under the yellow splat?

Take 10 cards numbered 0 to 9.



Pick 3 cards with a total of 12.  
You can do it in 10 different ways.  
How many can you find?

# YOHAKU PUZZLE

Grade 3

You will need three addends to make each sum.

You can only use the numbers  
1, 2, 3, 4, 5, 6, 7, and 8

How many solutions can you find?

			12
			13
			11
10	12	14	+

# SOLVE ME MOBILES

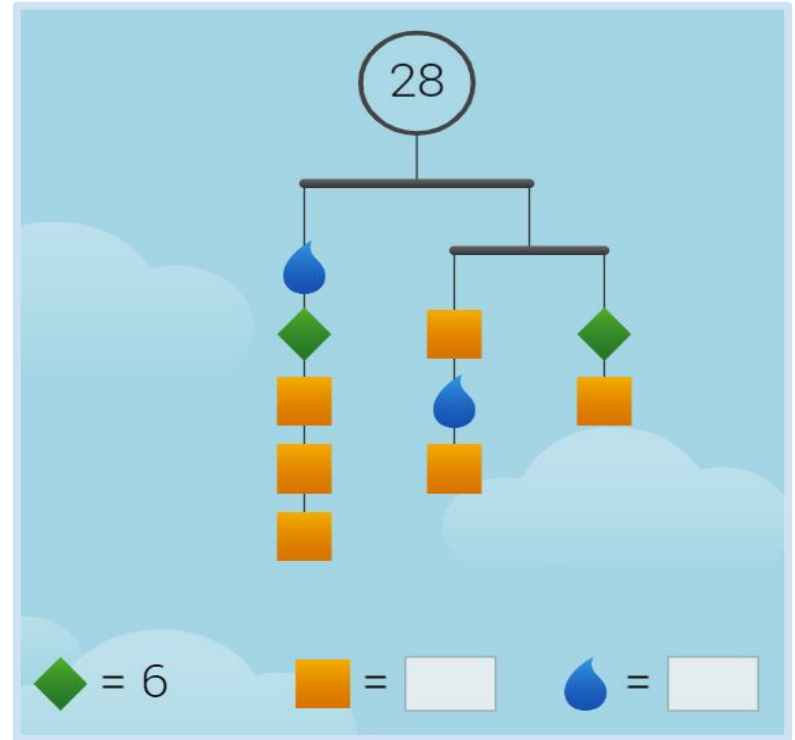
Grade 4

How do these Mobile Puzzles work?

The Mobile is balanced which means each side of the mobile is the same value. You need to figure out what each shape is worth in order to get the total. Each shape is a different whole number.

THERE IS ONLY 1 SOLUTION.

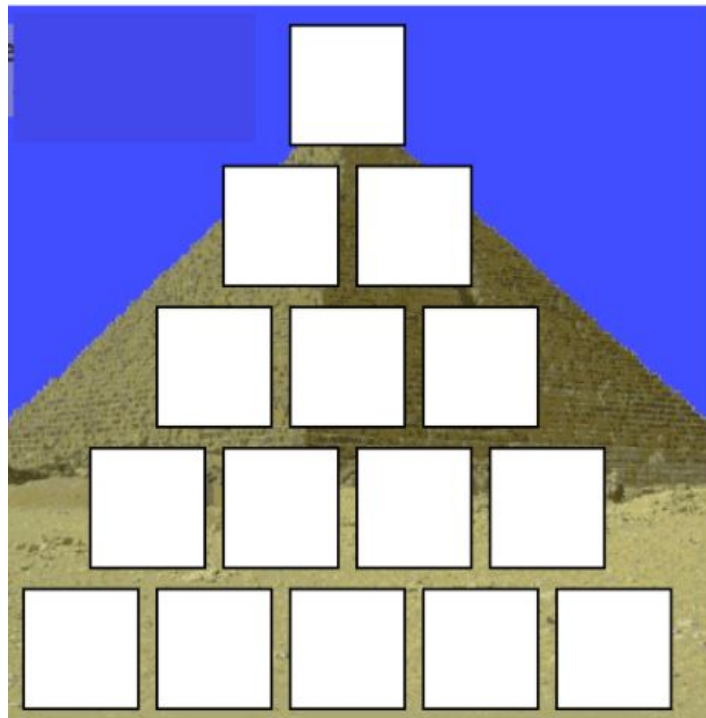
What is the value of the following:



# Pyramid Puzzle - Building Up

Grade 5

You are going to put the numbers 1 to 5 in the bottom row of this pyramid. They can be arranged in any order. The numbers in the other bricks are found by adding the two bricks immediately below together. The challenge is to find the arrangement of the numbers 1-5 in the bottom row that gives the largest total in the top brick of the pyramid.



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# Using Curricular Materials

*Focusing on the standard you are teaching  
helps you identify the task.*

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# Grade 5 Example

The Eureka book suggested teachers call on students one operation at a time to provide an example of how they would use each operation in the situations they had brainstormed as a class.

The teacher fills in the anchor chart while student provide word problems. Repeat for 2 or 3 situations.

Situation	Add	Subtract	Multiply	Divide
Baking cookies	Find the total number of cookies.	How many cookies are left after you eat some?	There are _____ times as many chocolate chip cookies as sugar cookies.	How many cookies can each person have?
Organizing pencils	Find the total number of pencils.	How many pencils are left after another class borrows some?	There are _____ times as many purple pencils as blue pencils.	How many pencils can go in each bin?
Counting money	How much money do you have in all?	If you spend some money, how much money is left?	Find the amount of money it costs to buy _____ sandwiches.	Find the amount of money each person gets if it is divided equally.
Riding the subway	Find the total number of people in the subway car.	How many people are still on the subway car after _____ people get off?	If there are _____ people in each car of the train, how many people are on _____ cars?	If there are _____ people altogether in _____ cars, and the same number of people are in each car, how many people are in each car?

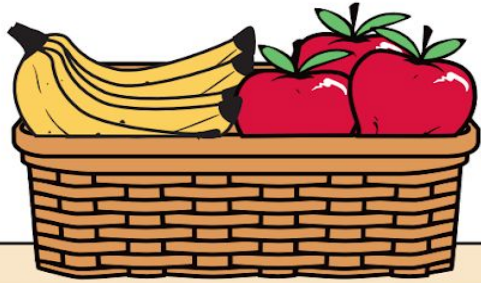
# Instead.....

I put the students into random groups using the playing cards. They were asked to create word problems for one situation across all four operations.

We came back together and I called on groups to share one specific story for each situation. I had preselected some of the stories I wanted to be shared.

Situation	Add	Subtract	Multiply	Divide
Baking Cookies				
Riding the Subway				
Counting Money				

# Grade 2 Example



Banana  
60¢

Apple  
50¢



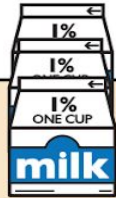
Chips  
65¢



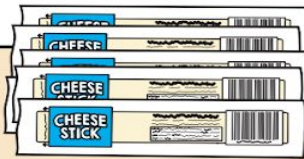
Crackers  
70¢



Juice  
75¢



Milk  
55¢



Cheese Stick  
45¢



Fruit Chew  
10¢



Ginger Candy  
15¢



Peppermint Patty  
25¢



Lollipop  
35¢



Licorice  
30¢



Fish Cracker  
1¢

## Grade 4 Example

Folding chairs are set up for a school play.

There are 16 rows of chairs, each with 28 chairs.

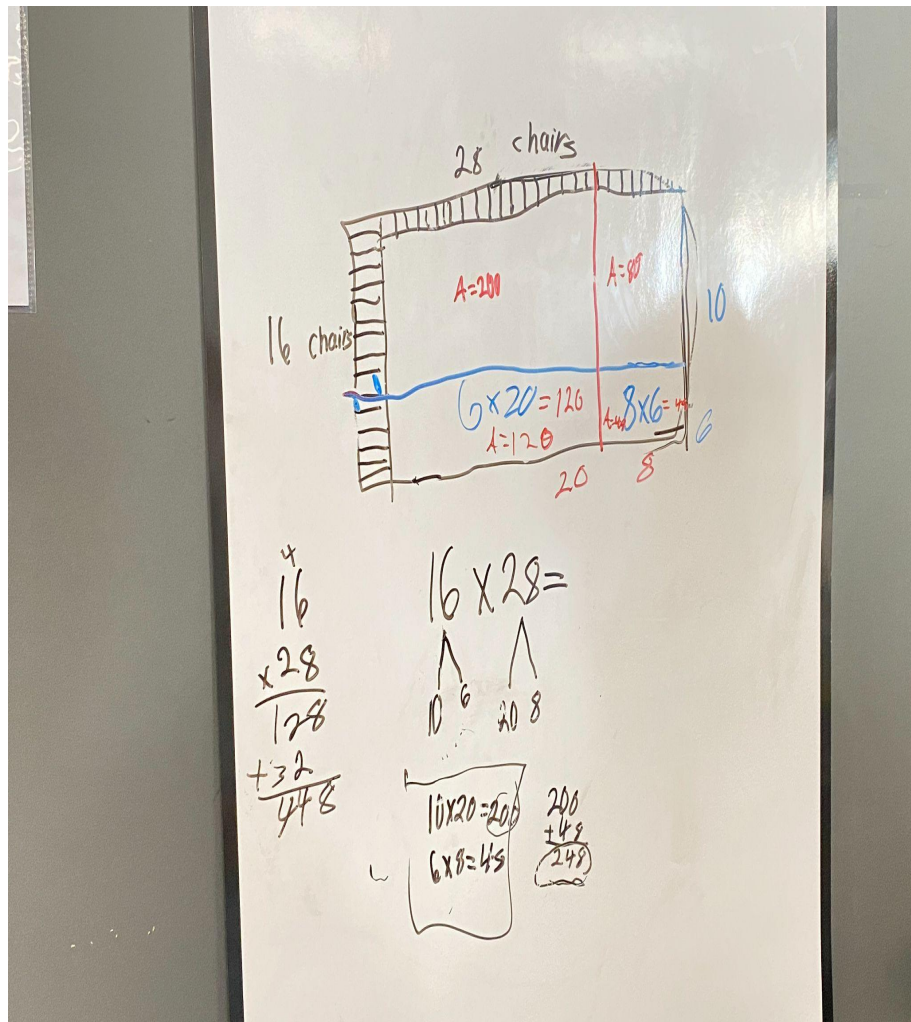
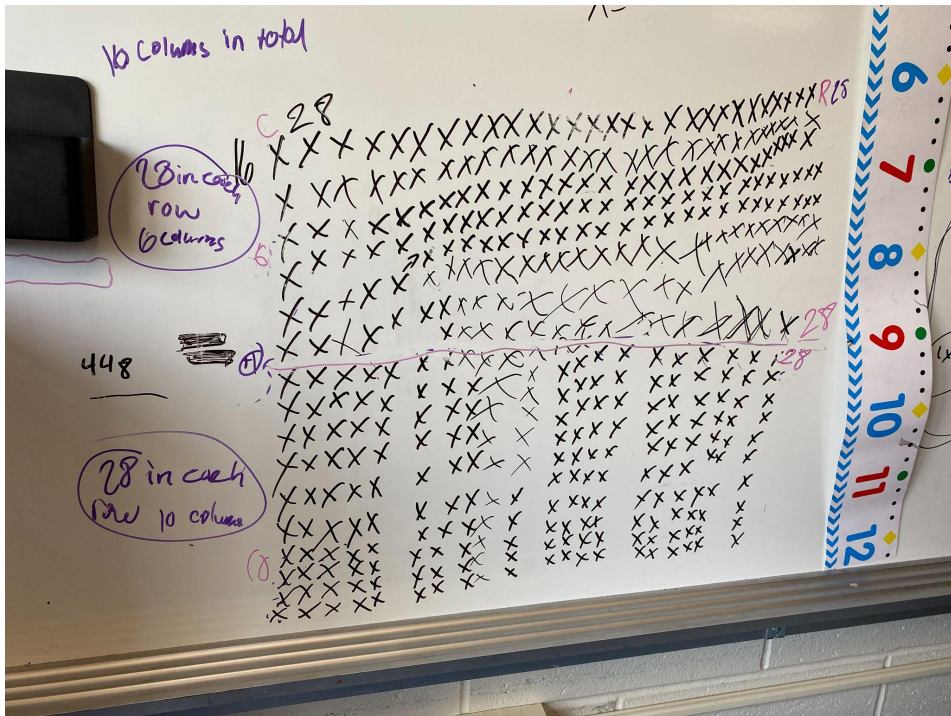
How many folding chairs are there?

**The answer is 448 chairs.**

Can you use only multiplication to prove the answer is correct?



# Grade 4 students "discover" the area model



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# Discourse

*Talking helps people think and helps  
students learn to think.*

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**WHEN A STUDENT  
RECOGNIZES THEY DON'T  
KNOW SOMETHING, IT  
SHOULD BE A TRANSITION  
TO KNOWING, NOT A  
TERMINATION OF  
THINKING.**

Connie Hamilton

# NCTM Definition

Discourse is the **mathematical communication** that occurs in a classroom. Effective discourse happens when **students articulate their own ideas** and seriously **consider their peers' mathematical perspectives** as a way **to construct mathematical understandings**. Encouraging students to **construct their own mathematical understanding through discourse** is an effective way to teach mathematics, especially since the role of the teacher has transformed from being a **transmitter of knowledge to one who presents worthwhile and engaging mathematical tasks**.

# Does this create engagement?

In the traditional classroom, students **answer questions**; they **don't usually ask them**. For years, students have sat in classrooms where the **teachers ask the questions to which they already know the answer**.

# #ThinkingClassroom

10 Things to Say in Response to a Proximity or Stop-Thinking Question

Isn't that interesting?

Can you find something else?

Can you show me how you did that?

Does that make sense?

Are you sure?

Is that always true?

Why don't you try something else?

Why do you think that is?

Why don't you try another one?

Are you asking me or telling me?

Author: @pglijedahl

Graphic: @wheeler\_laura

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## Questioning: Who is doing the asking?

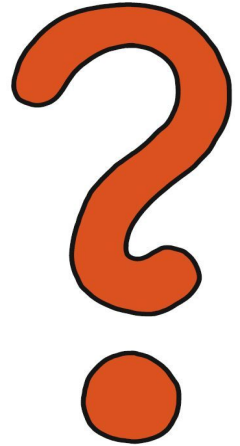
Good thinkers are good questioners, and with many students, this skill does not happen automatically or by accident. In a thoughtful classroom, the **encouragement of student questions** is very important.

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# Productive Struggle

**Genuine perplexity**, which is at the **root of all learning**, is rarely admitted by students. **Risk** is involved in **caring about something enough to confess lack of knowledge about it.**

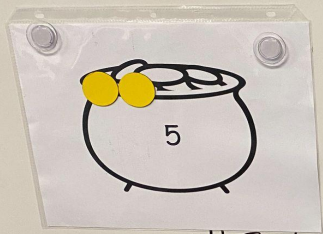
Creating an environment in which students **freely question** subject matter, the teacher, and each other is **critical for developing thinking.**



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# Student Work Examples

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$$\begin{aligned} 5 - 4 &= 1 \\ 5 - 3 &= 2 \\ 5 - 2 &= 3 \end{aligned}$$

$$5 - 5 = 0$$

$$5 - 5 = 0$$

$$5 - 4 = 1$$

$$5 - 4 = 1$$

$$5 - 4 = 1$$



BLO



RAP



RAP



BLO



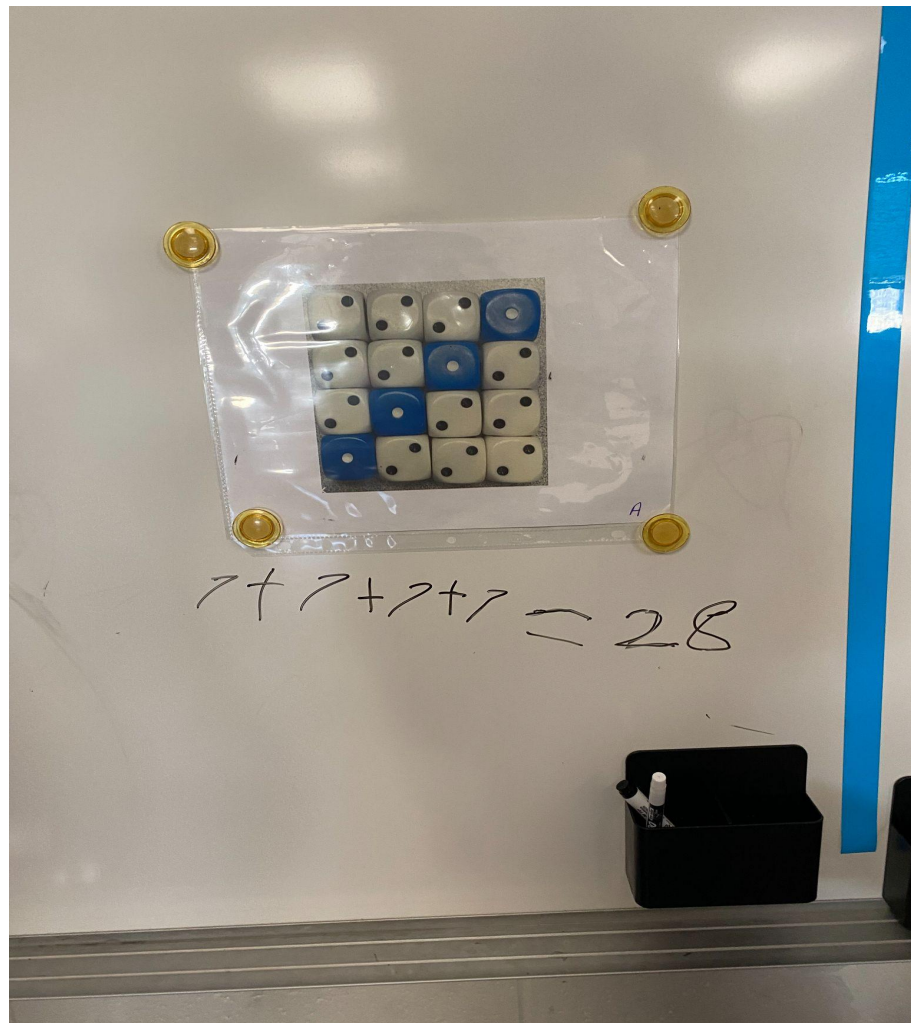
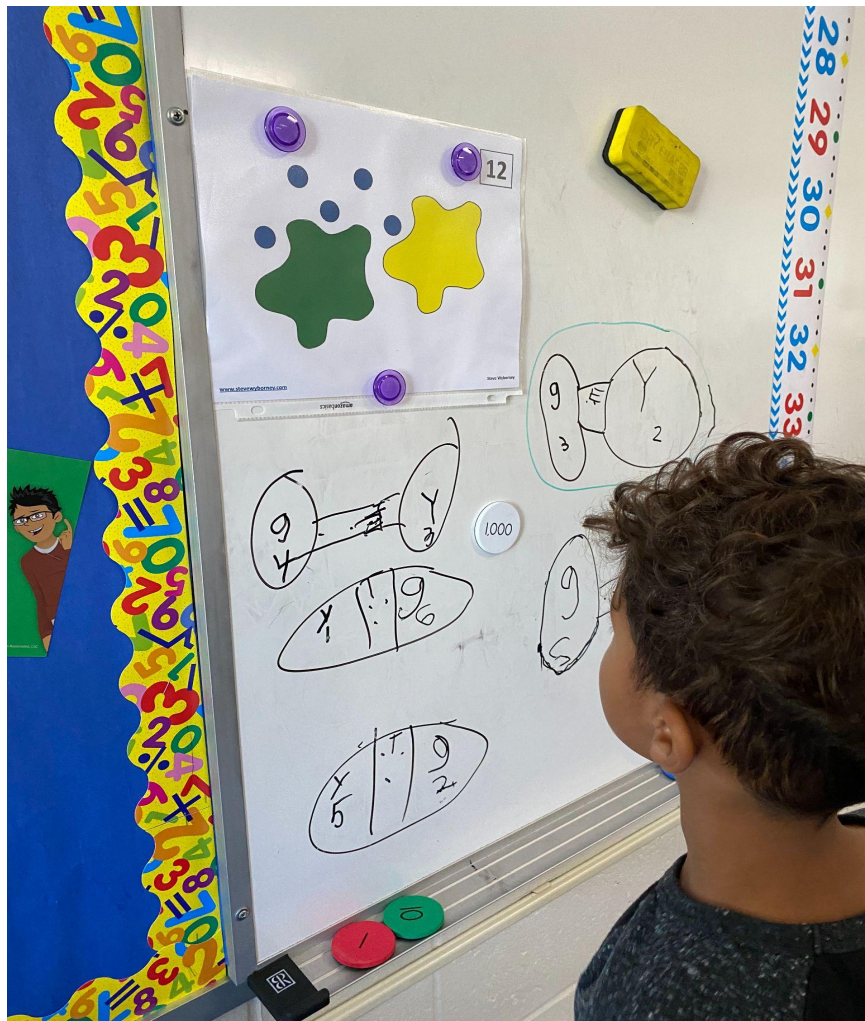
RAP

5 +

5 =

5







Things got a little crazy in the North Pole as Santa got ready to deliver presents. The reindeers and elves were all mixed up. Santa counted 22 legs. How many reindeer and elves could there be?



$$2x + 2y = 22$$

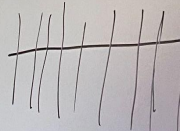
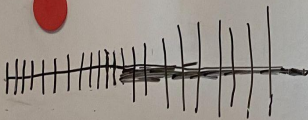


elves  
3  
4  
-

reindeere  
4  
3  
5

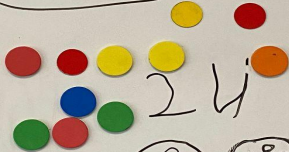


4 e i l

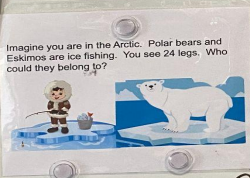


12 Eskimos.

9 Polar bears.



24

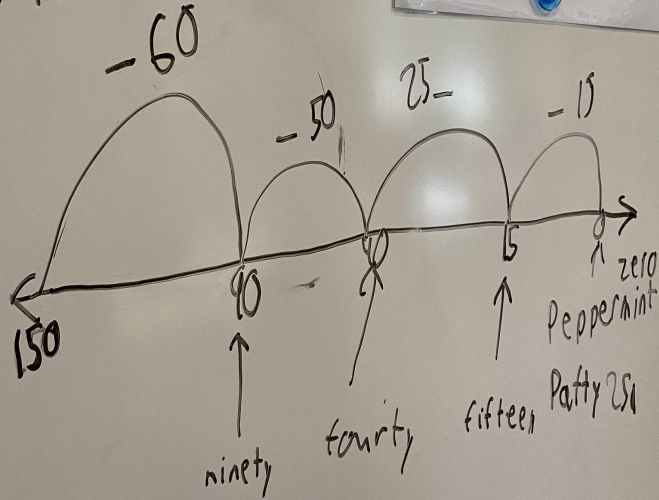


$$4 + 4 + 2 + 2 + 4 + 2 + 4 + 2 = 24$$





150 became 50 ↓  
Apple 50 ↓ number jump



Use the Read, Draw, Write process to solve.

64 kids have milk with lunch.

27 kids have punch.

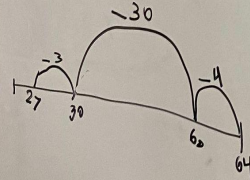
How many more kids have milk than punch?

There are 37 Milk With lunch  
Then punch

$$60 - 20 = 40$$

$$4 - 7 = -3$$

$$40 - 3 = 37$$



Graphic Organizer: Change Problems (Add To)

Beginning: 64 → Change + or -: - ? → Ending: 27

Equation:

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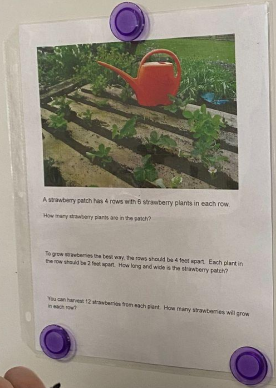
Graphic Organizer: Change Problems (Add To or Take From)

Beginning: ○ → Change + or -: ○ → Ending: ○

Equation:

$$16 \times 10 = 160$$

$$16 \times 6 =$$



$$6 \times 9 = 24$$



Alex has \$273  
to buy farming supplies.

\$0 left

Handwritten calculations and lists on the whiteboard:

$$\begin{array}{r} 180 \\ + 91 \\ + 91 \\ \hline 273 \end{array}$$

$273 - 90 = 233$  (Washer)  
 $233 - 79 = 154$  (Bed)  
 $154 - 10 = 144$  (Compost)  
 $144 - 10 = 134$  (Compost)  
 $134 - 5 = 129$  (Compost)  
 $129 - 10 = 119$  (Compost)  
 $119 - 10 = 109$  (Compost)  
 $109 - 10 = 99$  (Compost)  
 $99 - 10 = 89$  (Compost)  
 $89 - 10 = 79$  (Compost)  
 $79 - 10 = 69$  (Compost)  
 $69 - 10 = 59$  (Compost)

Page 1: Garden Washing Station, Wooden Raised Bed, Compost, Wooden Planters, Compost  
 Page 2: Wooden Raised Bed, Washing Station, Compost, Compost

154 - 10 (Compost) = 144  
 144 - 10 = 134  
 134 - 5 = 129  
 129 - 10 = 119  
 119 - 10 = 109  
 109 - 10 = 99  
 99 - 10 = 89  
 89 - 10 = 79  
 79 - 10 = 69  
 69 - 10 = 59

50 (Planters) + 10 (Compost) = 60  
 60 + 10 (Compost) = 70  
 70 + 10 (Compost) = 80  
 80 + 10 (Compost) = 90  
 90 + 10 (Compost) = 100  
 100 + 10 (Compost) = 110  
 110 + 10 (Compost) = 120  
 120 + 10 (Compost) = 130  
 130 + 10 (Compost) = 140  
 140 + 10 (Compost) = 150  
 150 + 10 (Compost) = 160  
 160 + 10 (Compost) = 170  
 170 + 10 (Compost) = 180  
 180 + 10 (Compost) = 190  
 190 + 10 (Compost) = 200  
 200 + 10 (Compost) = 210  
 210 + 10 (Compost) = 220  
 220 + 10 (Compost) = 230  
 230 + 10 (Compost) = 240  
 240 + 10 (Compost) = 250  
 250 + 10 (Compost) = 260  
 260 + 10 (Compost) = 270  
 270 + 10 (Compost) = 280



COLOURING GUIDE: Before using the parts and putting them into the good parts, Rose needs to sort the parts and put them into the good parts. He wants Rose to sort the parts into 3 bins. He wants Rose to have more than 80 items in 2 bins. He wants to have close to the same number of items in each bin.

My Robot Parts

Fluorescent Tube	216	Wire	88
Switch	178	Switch	178
Screw	341	Wire	88
Piece of Wire	160	Switch	178
Fluorescent Tube	216	Wire	88

How could Rose sort his parts into the bins?

pieces of wire

SCREW = 426

$$\begin{array}{r} 85 \\ +86 \\ \hline 171 \\ 85 \\ +86 \\ \hline 171 \\ 85 \\ +86 \\ \hline 171 \\ 85 \\ +86 \\ \hline 171 \end{array}$$

$$\begin{array}{r} 160 \\ +160 \\ \hline 320 \\ +80 \\ \hline 400 \end{array}$$

$$\begin{array}{r} 170 \\ +170 \\ \hline 340 \end{array}$$

$$\begin{array}{r} 28 \\ +78 \\ \hline 106 \\ +78 \\ \hline 184 \end{array}$$

$$\begin{array}{r} 172 \\ +172 \\ \hline 344 \\ +86 \\ \hline 430 \end{array}$$

$$\begin{array}{r} 85 \\ +85 \\ \hline 170 \\ +85 \\ \hline 255 \\ +85 \\ \hline 340 \end{array}$$

$$\begin{array}{r} 171 \\ +85 \\ \hline 256 \\ +85 \\ \hline 341 \end{array}$$

$$\begin{array}{r} 244 \\ +88 \\ \hline 332 \end{array}$$

100 pieces

Switch = 178

$$\begin{array}{r} 80 \\ +80 \\ \hline 160 \end{array}$$

Fuses - 216

$$\begin{array}{r} 175 \\ +75 \\ \hline 250 \\ +65 \\ \hline 315 \end{array}$$

$$\begin{array}{r} 135 \\ +75 \\ \hline 210 \end{array}$$

3 bins  
71 = 1 box  
72 = 1 box  
73 = 1 box  
Fuses

$$\begin{array}{r} 244 \\ +88 \\ \hline 332 \end{array}$$

Wire  
88  
78  
78  
88

$$\begin{array}{r} 87 \\ +86 \\ \hline 173 \end{array}$$

$$\begin{array}{r} 73 \\ +70 \\ \hline 143 \end{array}$$

$$\begin{array}{r} 171 \\ +73 \\ \hline 244 \end{array}$$

$$\begin{array}{r} 144 \\ +72 \\ \hline 216 \end{array}$$

Wire  
78  
78  
88  
88

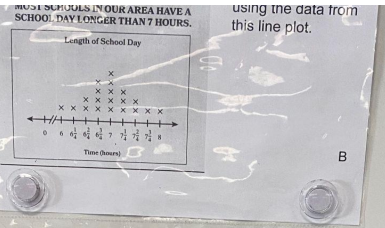
Fuses  
71  
72  
73

Switches  
89  
89

89: 1 box  
89: 1 box

Switches

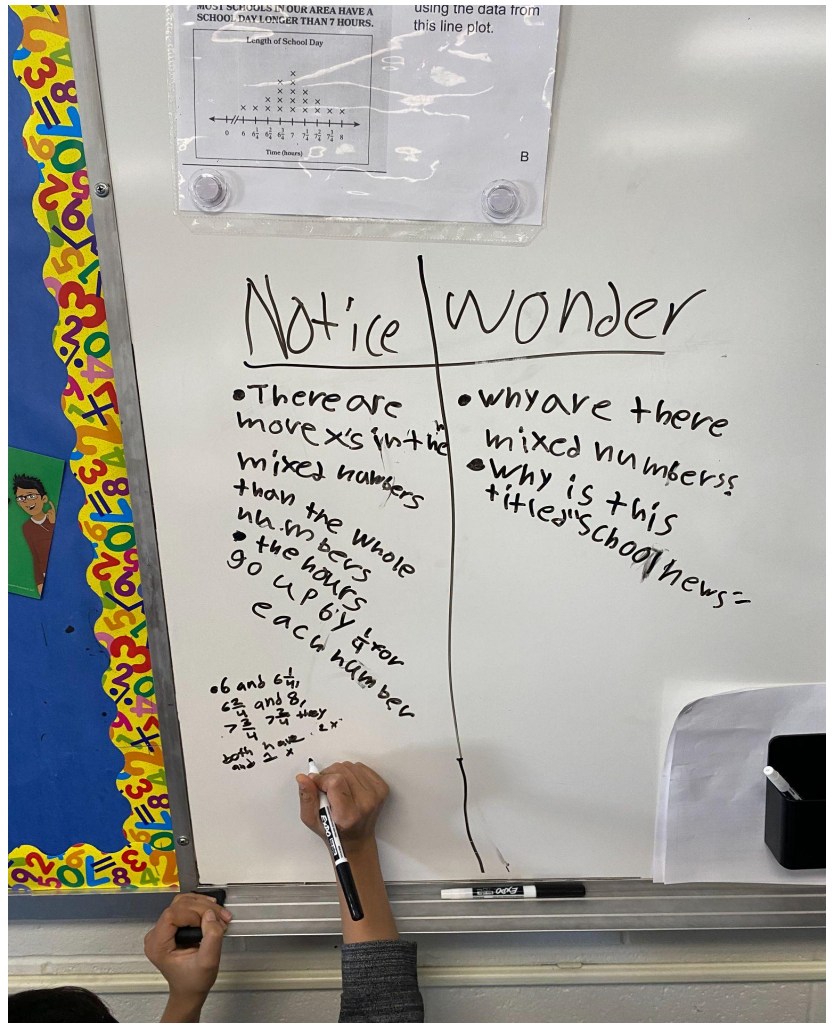
Jacqueline  
Benji Bella



# Notice Wonder

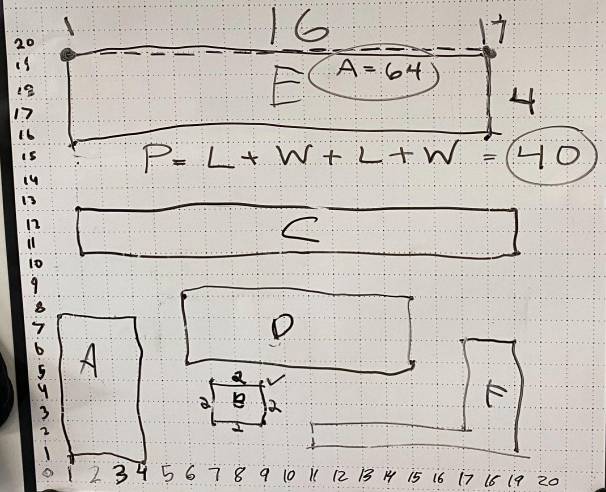
- There are more x's in the mixed numbers than the whole numbers
- Why are there mixed numbers?
- Why is this titled "School News"?
- The whole numbers go up by 1 for each number

6 and 6/10  
7 and 7/10  
8 and 8/10  
9 and 9/10  
10 and 10/10



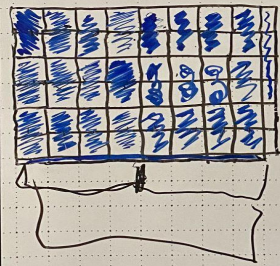


$$17 - 1 = 16$$



$$\begin{array}{r}
 13.65 \\
 \times 24 \\
 \hline
 54.60 \\
 +273.00 \\
 \hline
 327.60
 \end{array}$$

G.O. & his Neighbors can plant 24 shrubs and all the shrubs together will need 30 gal-  
 tons of water.  
 The amount of money heeded will be \$327.60 in all.



$$24 \times \frac{1}{4} = 24 \frac{24}{4}$$

$$\downarrow$$

$$30$$

# By: Jet Milo Ryan

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# Thoughts from Students

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# What I like about coming to the math lab is.....

- “doing the math that challenges my mind and brain.”
- “doing problems with friends,”
- “that I can work with new people and if I make a mistake the other people in my group will help me so I don't get the whole question wrong.”
- “all the math. It make me HAPPY HAPPY HAPPY.”
- “I get to see what other people think about the problem cause everyone has a different brain and different strategies. Also, when I share my answer and strategies most of the time they agree with me and sometimes they don't.”
- “it's way more fun in the math lab than math in the classroom.”



**THE BEST ANGLE  
FROM WHICH  
TO APPROACH  
A PROBLEM IS THE  
TRY ANGLE**





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# Thoughts from Teachers

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# Teachers share their new learnings & reflections

- “I have always paired students with so much thought behind each pairing, but in the lab, I was amazed as to how the **random partnerships showed different abilities**. Students showed skills that I may not have noticed if not for the lab.”
- “The math lab has really taught me to **stand back and give more think/wait time**. I often want to jump in and help “teach” the students the way to solve problems, but I’ve learned how valuable it is to stand back and let the students work it out. **They are capable of SO much!**”
- “I am blown away by the skills that I have seen Kindergarten students use in the math lab. The children have **expanded their critical thinking skills beyond what I have ever seen in past years**. They work well together and learn so much from each other! They get so excited when I say we are going to the math lab!”
- “**As a teacher I have grown in my ability to sit back and let thinking happen**. By giving the students time to figure it out, they continue to surprise me with what they do, how they get to an answer, and **how they communicate their thinking**. They come up with ways to show their thinking that I would not have thought of. “

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# Instructional Rounds

## *Observer Noticings*

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# Capturing Student Thinking & Discourse

- Student: “You don’t have to use a math tool, you can visualize it.”
- All students did not always agree, but considered the mathematical perspective of each other.
- Students were critical of each other’s work: “Wait, but it’s not equal.”
- “What should we write next?” “Thirds” “We could do that” “We can do whatever we want in our work space.”
- Student: “We won’t have enough room if we draw it this way.”
- Students were able to ask other groups clarifying questions. One student thought her thinking was clear and realized that others needed more clarifications.
- Student : “We don’t have to be too complex.” (When considering which denominators to use.)

# Capturing Teacher Moves & Facilitation

- The teacher highlighted students who made mistakes to showcase learning opportunities.
- Teacher: “What does it mean when I say show more ways to do it?” Student: “There’s more than one way so everyone can be right.”
- Teacher: “Do you want to go back and revise this?”
- Teacher : “What are some things we do as mathematicians if we are stuck?”
- Teacher asked questions that allowed students to go back to the task and evaluate their thinking.
- To initiate the task, the teacher gave some examples to give all students access to the context.
- Teacher as a facilitator – open-ended questions/rephrasing.

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# Reflections/Suggestions

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# Some things I learned along the way

- Consider the students in your class/building and their needs
  - Student(s) in wheelchairs
  - Student(s) who might need to work in a quieter space
- Busy yourself away from the students for the first 5-7 minutes so they can talk through the task and get started without interruption
- Even our youngest students can work for 45-minutes if the task is engaging
- Always plan an extension
- Handing out the cards after the task was delivered worked better than when they came in the door
- Purchase plenty of expo markers and erasers
- Magnetic manipulatives are a must

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# Questions & Answers

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# Contact

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